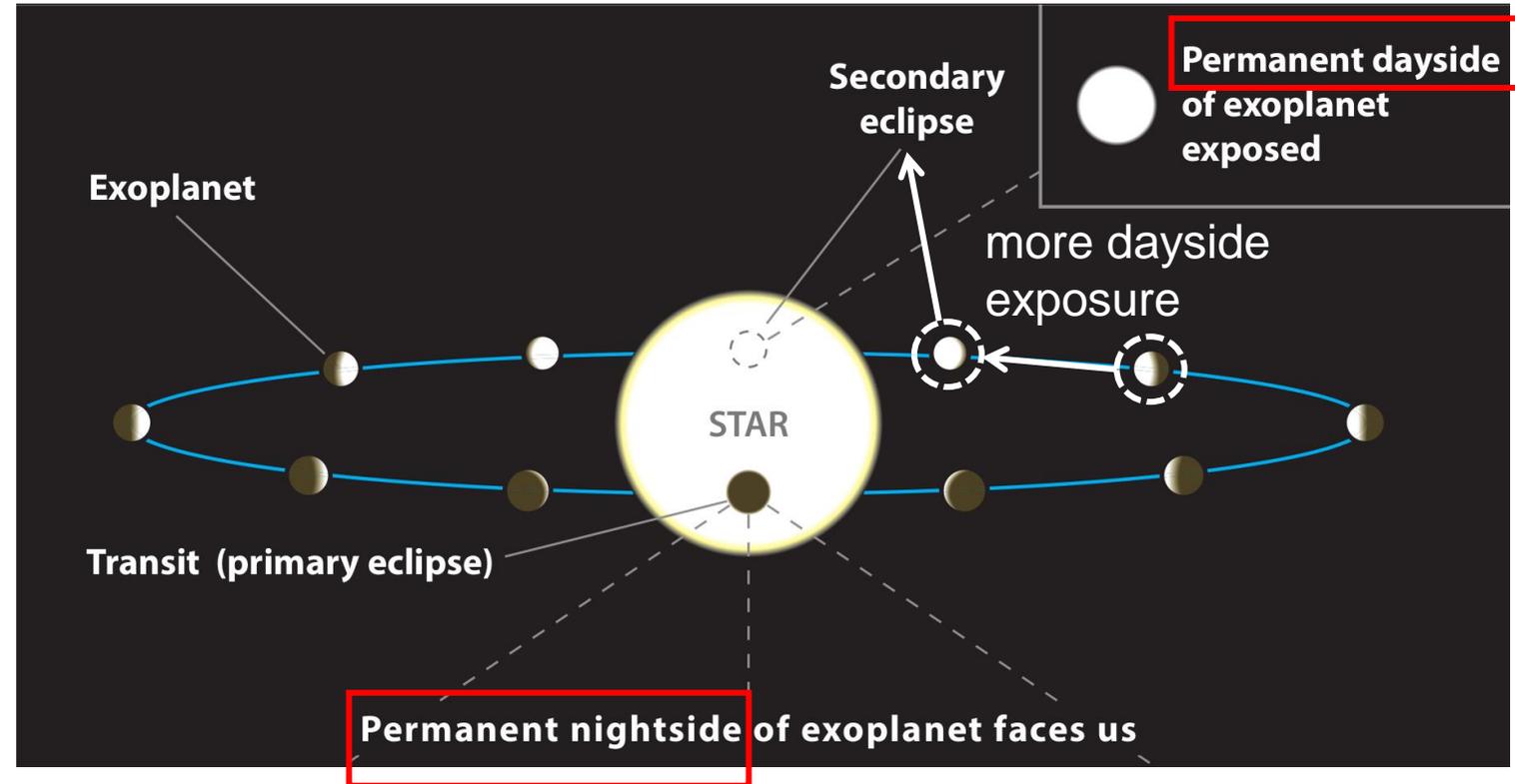
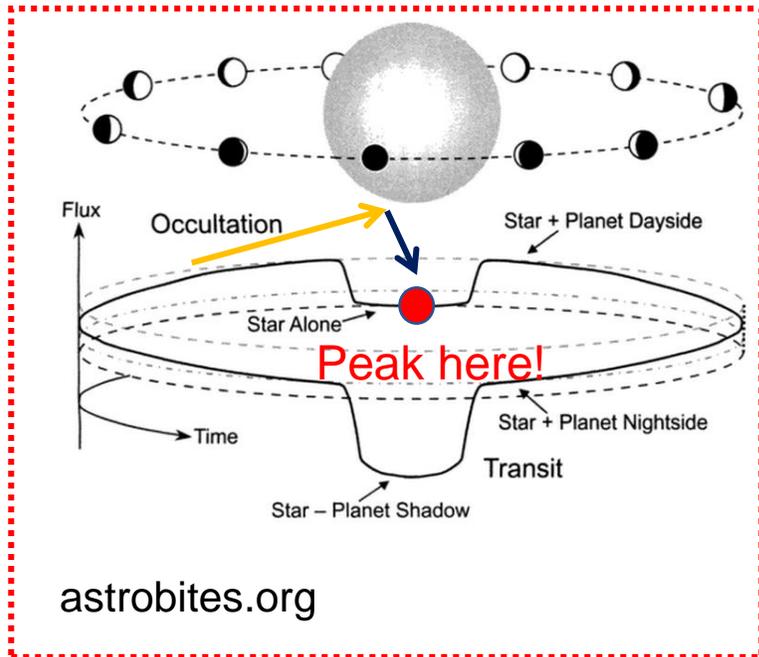


# Magnetically Driven Circulation and Hotspot Shift on Tidally- locked Hot Jupiters

Yu Wang & Cong Yu,  
SYSU  
2021/04/16

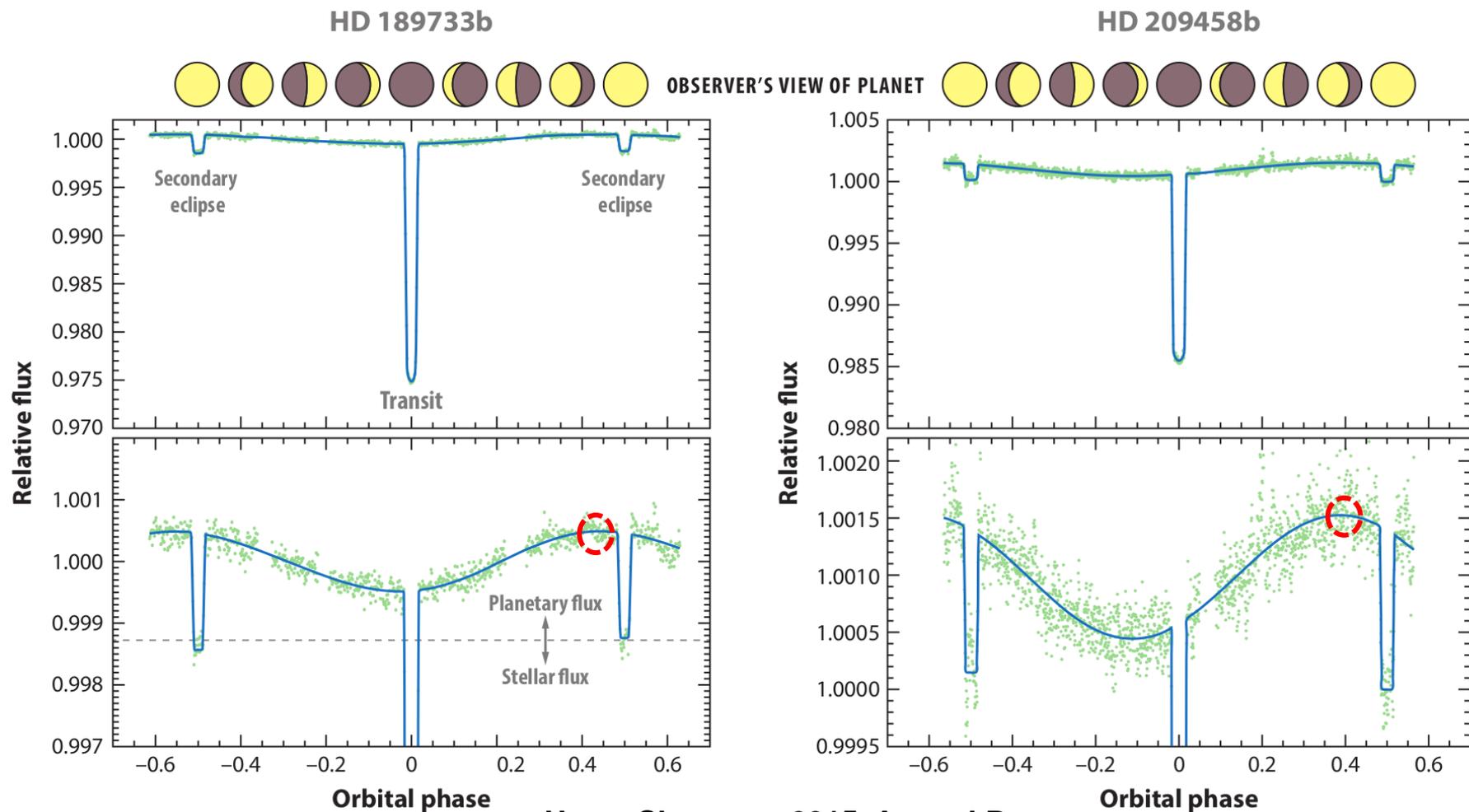
# Tidally-locked Hot Jupiters and Transit Method



Heng, Showman 2015, Annual Rev

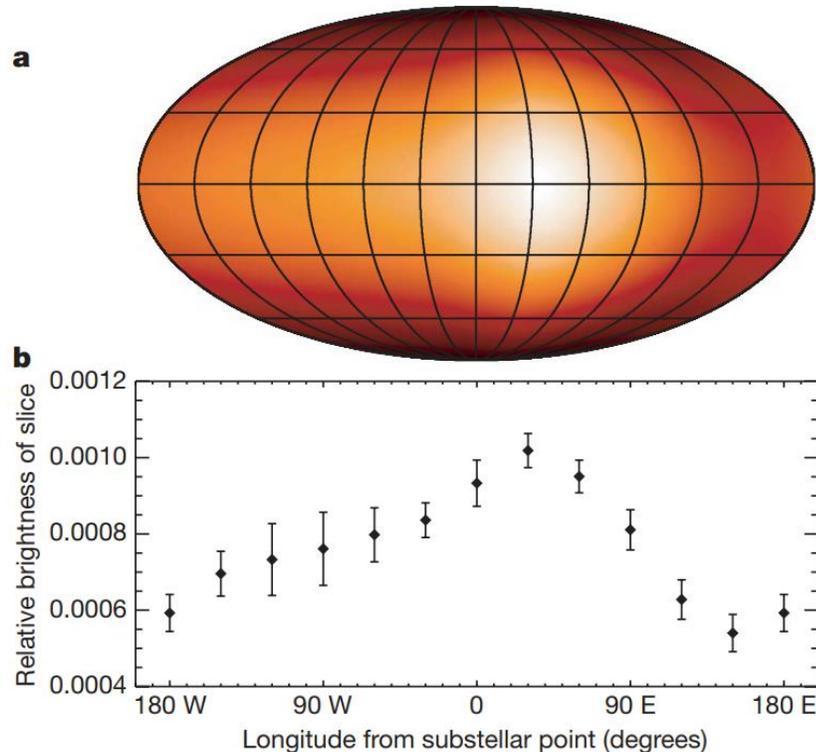
If we assume a tidally-locked planet with rocky, dry surface, then the brightest place (**hotspot**) on it should be the position where sun shines directly (**Substellar Point**), which means from light curve we should find planet's flux's peak **concide** with the Secondary eclipse.

# Phase Curve of 2 HJs



**Flux's peak position is earlier than the secondary eclipse.** -> hotspot not at substellar point

# HJ Atmosphere & Eastward Hotspot



**Knutson et.al 2007, nature**  
2D temperature mapping of HD 189733b's atmosphere. Hotspot is shifted **eastward** of the substellar point

What causes this feature?

Why in solar Jupiter we don't have this?

Rotation

Due to tidal damping, Hot jupiter rotates much slower.....

Jupiter: 10 hrs / Hot Jupiter: 3-5 days

Intense Day-Night heating gradient

Equator-pole heating gradient much dominating in solar system planets.

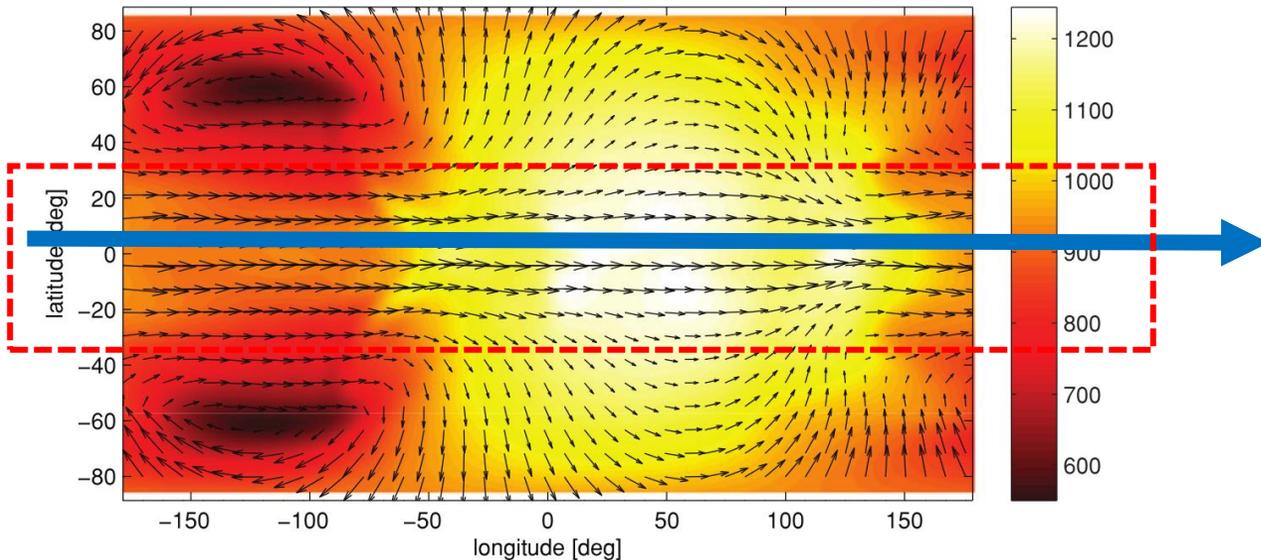
Internal heating

Comparable to stellar irradiation on Jupiter, but tiny on Hot Jupiter.

Highly-irradiated

~100 k on Jupiter, ~ 2000K on Hot Jupiter.  
Potentially ionized atmosphere.

# Superrotation



**showman et.al 2009, ApJ**  
GCM simulation of HD 189733b's atmosphere

A **common feature** in all simulations:

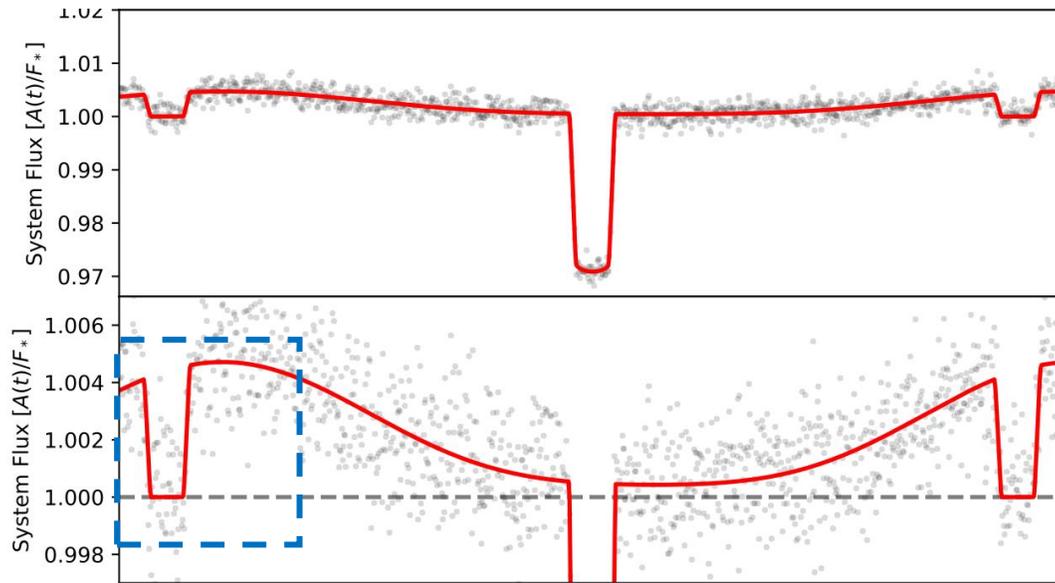
eastward hotspot together with a strong eastward equatorial **zonal wind**, we call it **Superrotation**.

Also been observed in HD209458b ~ 2km/s  
(ref: Snellen et al.2010)

Do all hot Jupiters have an eastward hotspot and eastward equatorial superrotation?

**No**

# Westward Hotspot: Diversity



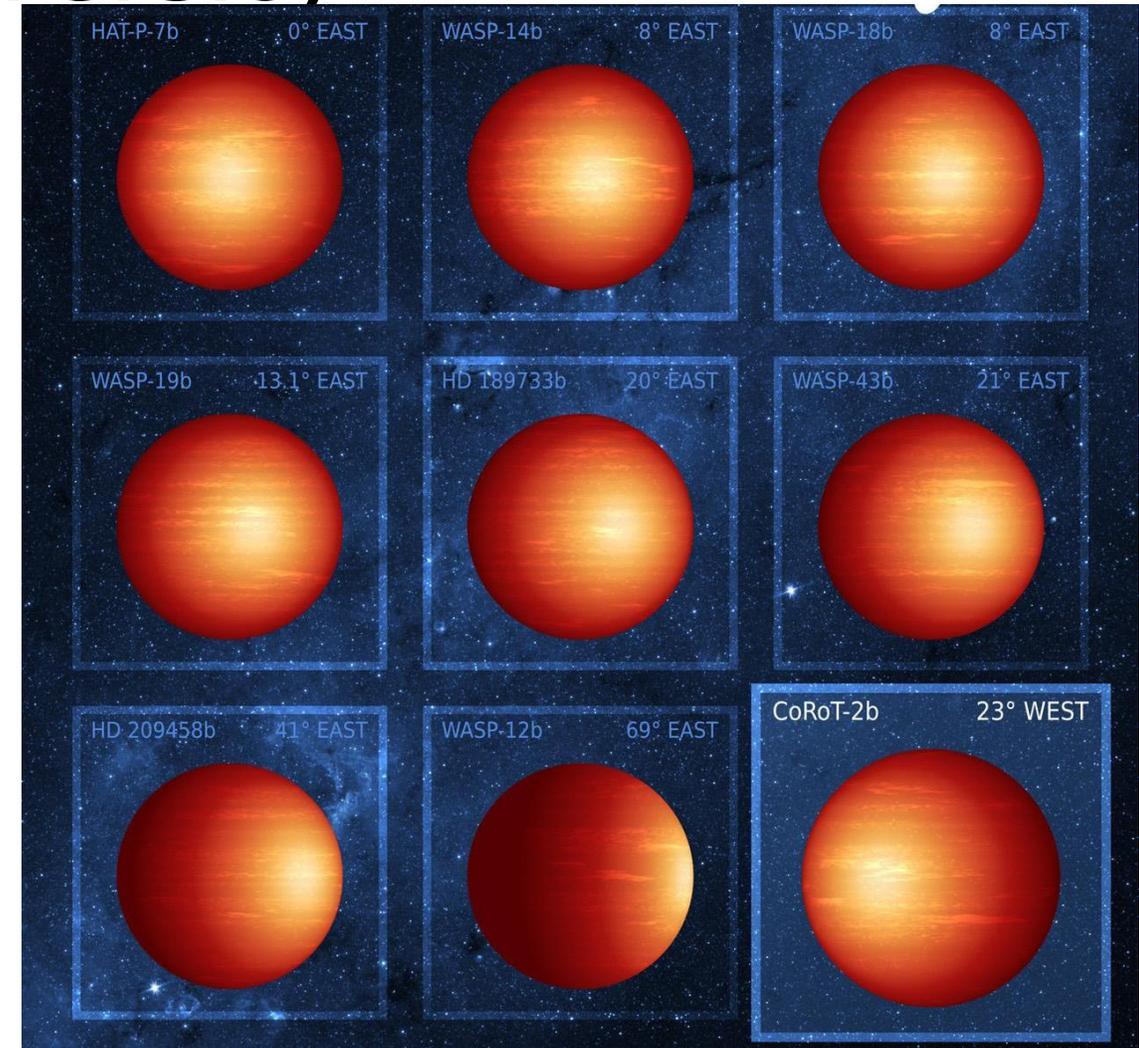
Lisa Dang et. al, 2018, Nature astro.

Phase curve peaks **after** the secondary eclipse.

-> **Westward hotspot.**

Why? New mechanism?

Published results



Lisa Dang, Future of Space Astronomy in Canada,  
Nov 6-7 2018 Université de Montréal, QC 6

# Westward Hotspot: Implications

Possible explanations:

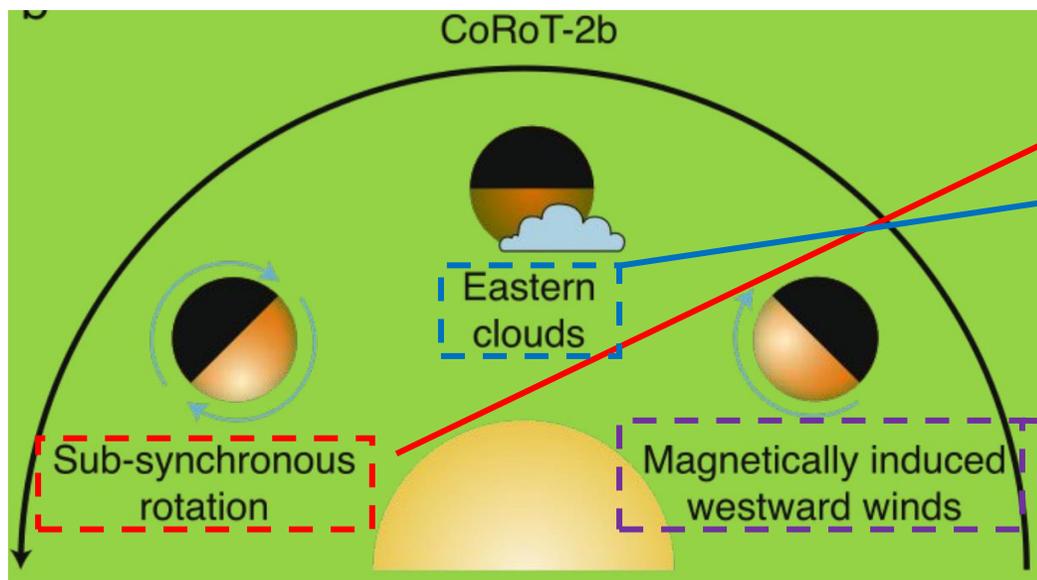


Illustration from Barstow (2018), Lisa Dang

Not totally tidally locked:  
Frequent planet-star angular momentum exchange? Why? Wrong understanding of tidally locked timescale?

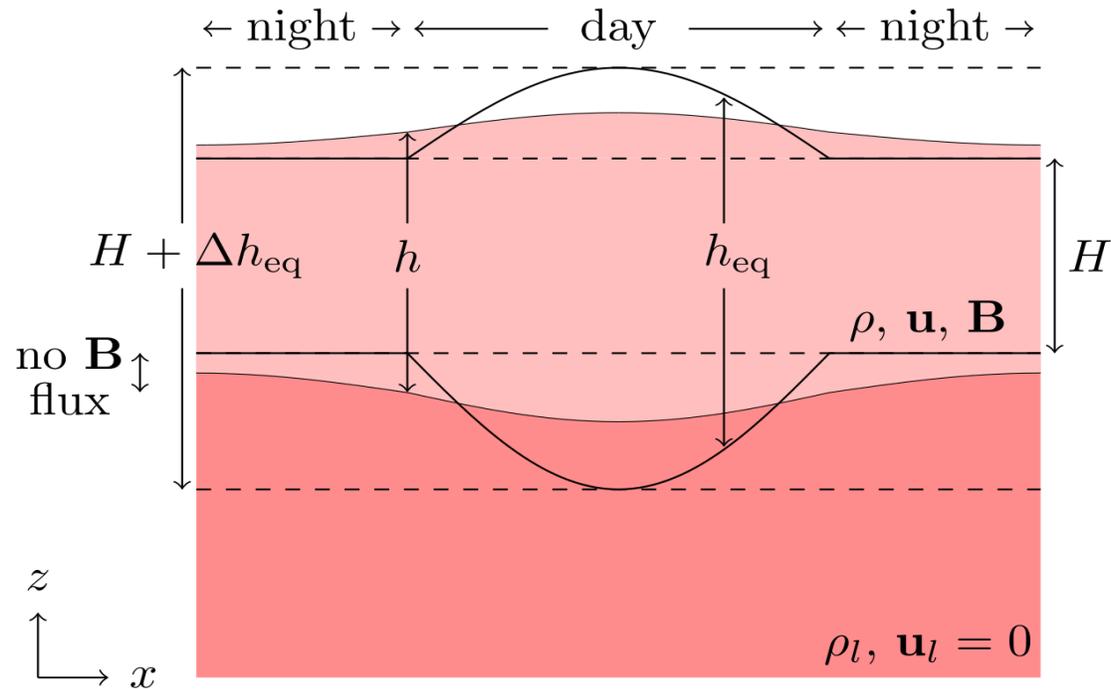
Formation mechanism? What's the impact on observations?

Magnetically driven westward wind, unknown mechanism.

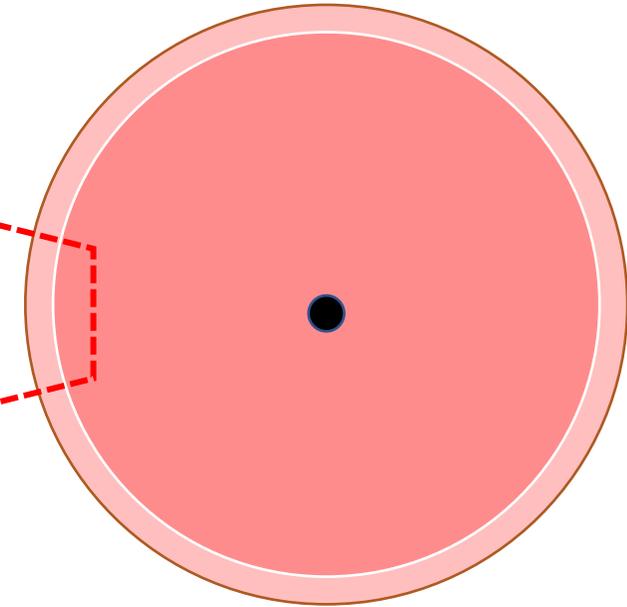
High irradiation implies weekly ionized atmosphere.

What we are interested in.

# Simplified Model



Hindle et. al, 2019, ApJL



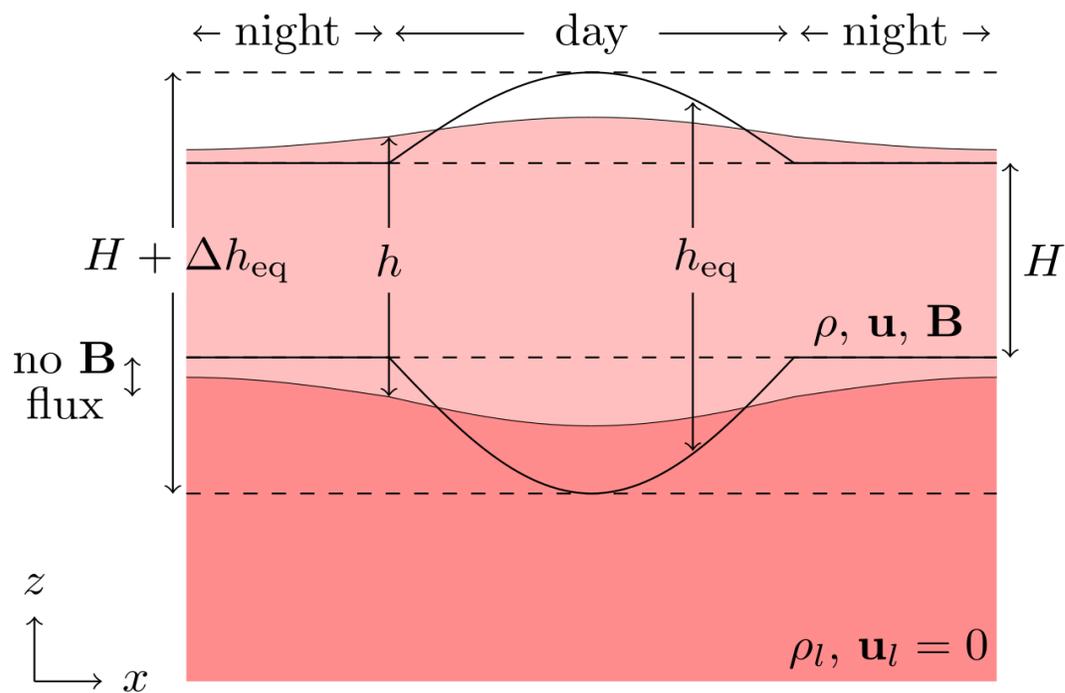
Pink: shallow, active upper layer

Red: deep, quiescent lower layer

Horizontal scale  $\gg$  vertical scale  $\rightarrow$  neglecting vertical variations  $\rightarrow$  column-integrated Euler equations  $\rightarrow$  2D shallow water equation

- Each layer has a constant density.
- Magnetic field can not go across the layer surface.

# Shallow water approximation



Hindle et. al, 2019, ApJL

$$\frac{d\mathbf{v}}{dt} + g\nabla h + \boxed{f\mathbf{k} \times \mathbf{v}} = \boxed{\mathbf{R}} - \boxed{\frac{\mathbf{v}}{\tau_{\text{drag}}}} + \boxed{(\mathbf{B} \cdot \nabla)\mathbf{B}}$$

Vertical momentum transport     Drag term     Magnetic tension

$$\frac{\partial h}{\partial t} + \nabla \cdot (\mathbf{v}h) = \boxed{\frac{h_{\text{eq}}(\lambda, \phi) - h}{\tau_{\text{rad}}}} \equiv Q$$

Newtonian relaxation type Thermal forcing

- All quantities 2D. e.g.  $h(x,y)$
- $h$ : Water Height ~ Pressure strength. ( $P \sim \rho gh$ ) ~ to mimic Temperature
- $h_{\text{eq}}$ : Gaussian / Cosine type. To mimic radiation equilibrium temperature.

# Hydrodynamic Mechanism: Free Waves

$$\frac{d\mathbf{v}}{dt} + g\nabla h + f\mathbf{k} \times \mathbf{v} = \mathbf{R} - \frac{\mathbf{v}}{\tau_{\text{drag}}}$$

$$\frac{\partial h}{\partial t} + \nabla \cdot (\mathbf{v}h) = \frac{h_{\text{eq}}(\lambda, \phi) - h}{\tau_{\text{rad}}} \equiv Q,$$

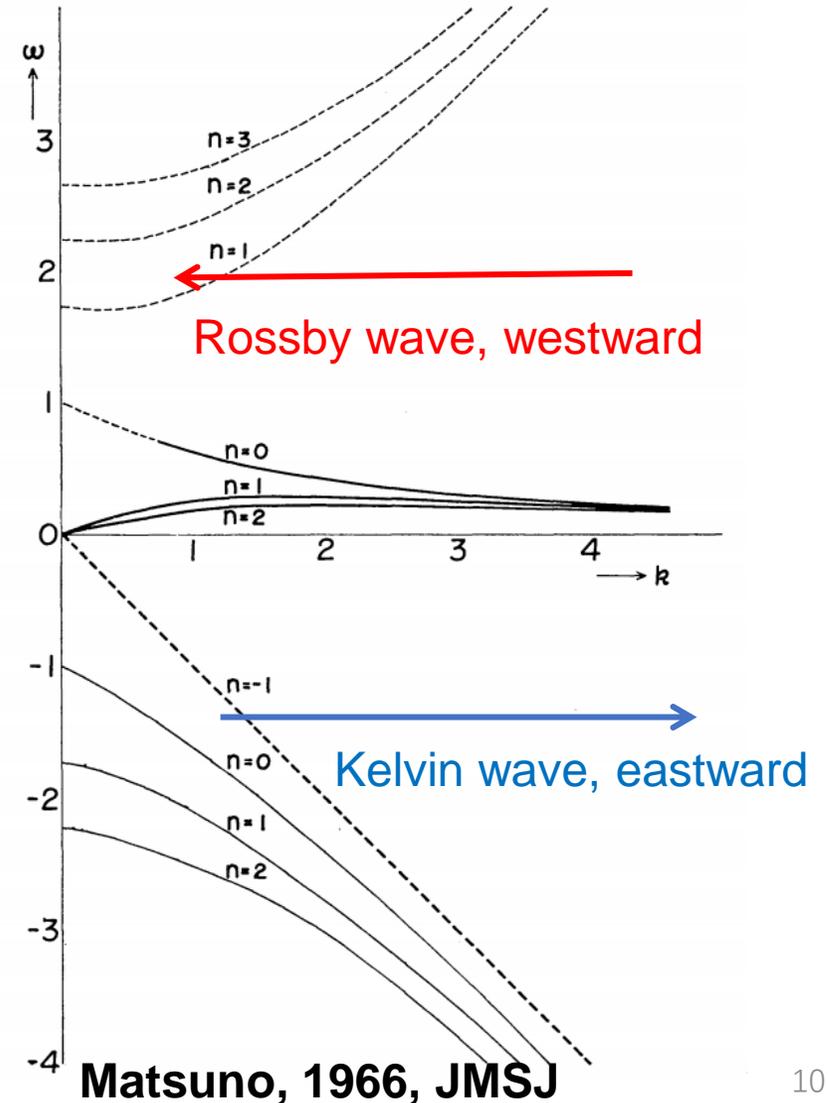
W/O thermal forcing, free system, we can do perturbations to gain wave modes.

e.g.,  $h = H + \eta \exp[i(\omega t + kx)]$

➔ dispersion relationship

$$\omega^2 - k^2 + \frac{k}{\omega} = 2n + 1 \quad (n=0, 1, 2, \dots)$$

Dispersion relationship



# HD Mechanism: Forced solution

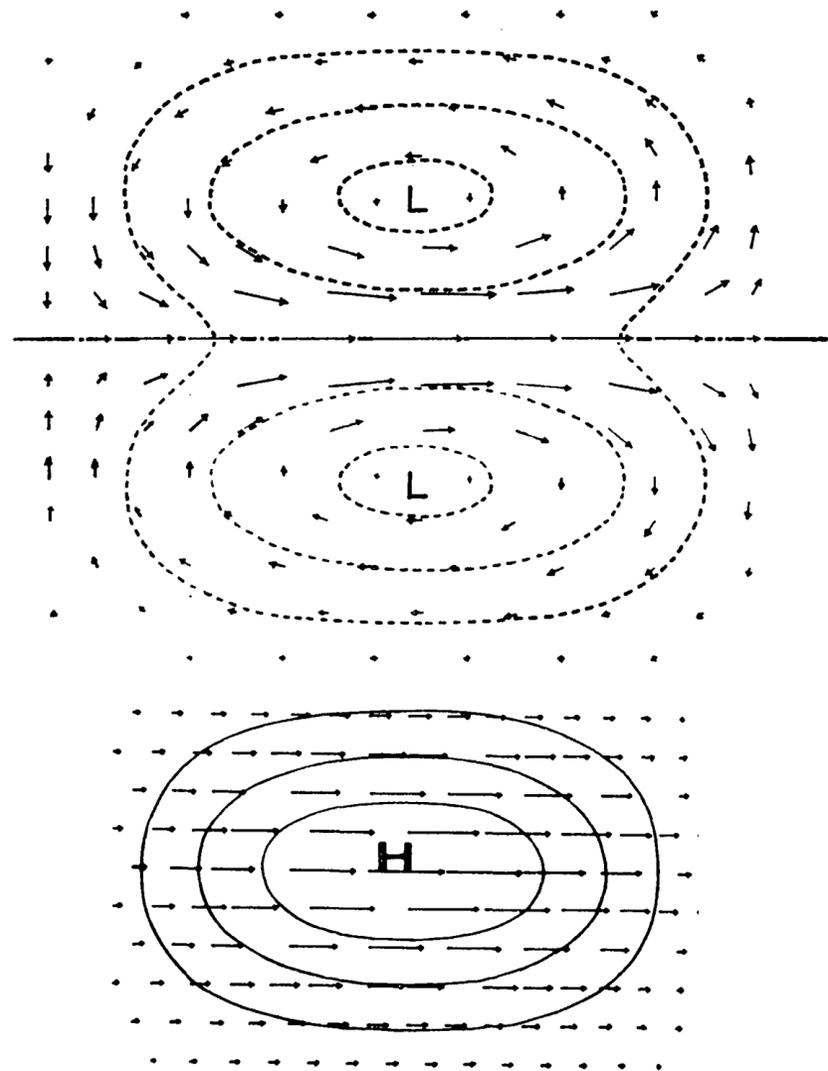
~~$$\frac{d\mathbf{v}}{dt} + g\nabla h + f\mathbf{k} \times \mathbf{v} = \mathbf{R} - \frac{\mathbf{v}}{\tau_{\text{drag}}}$$

$$\frac{\partial h}{\partial t} + \nabla \cdot (\mathbf{v}h) = \frac{h_{\text{eq}}(\lambda, \phi) - h}{\tau_{\text{rad}}} \equiv Q,$$~~

With thermal forcing, forced system, **We solve for steady state** of the perturbation.

Forced solution can be expanded by free wave modes.

On Hot Jupiters, driving force is the intense day-night heating gradient.



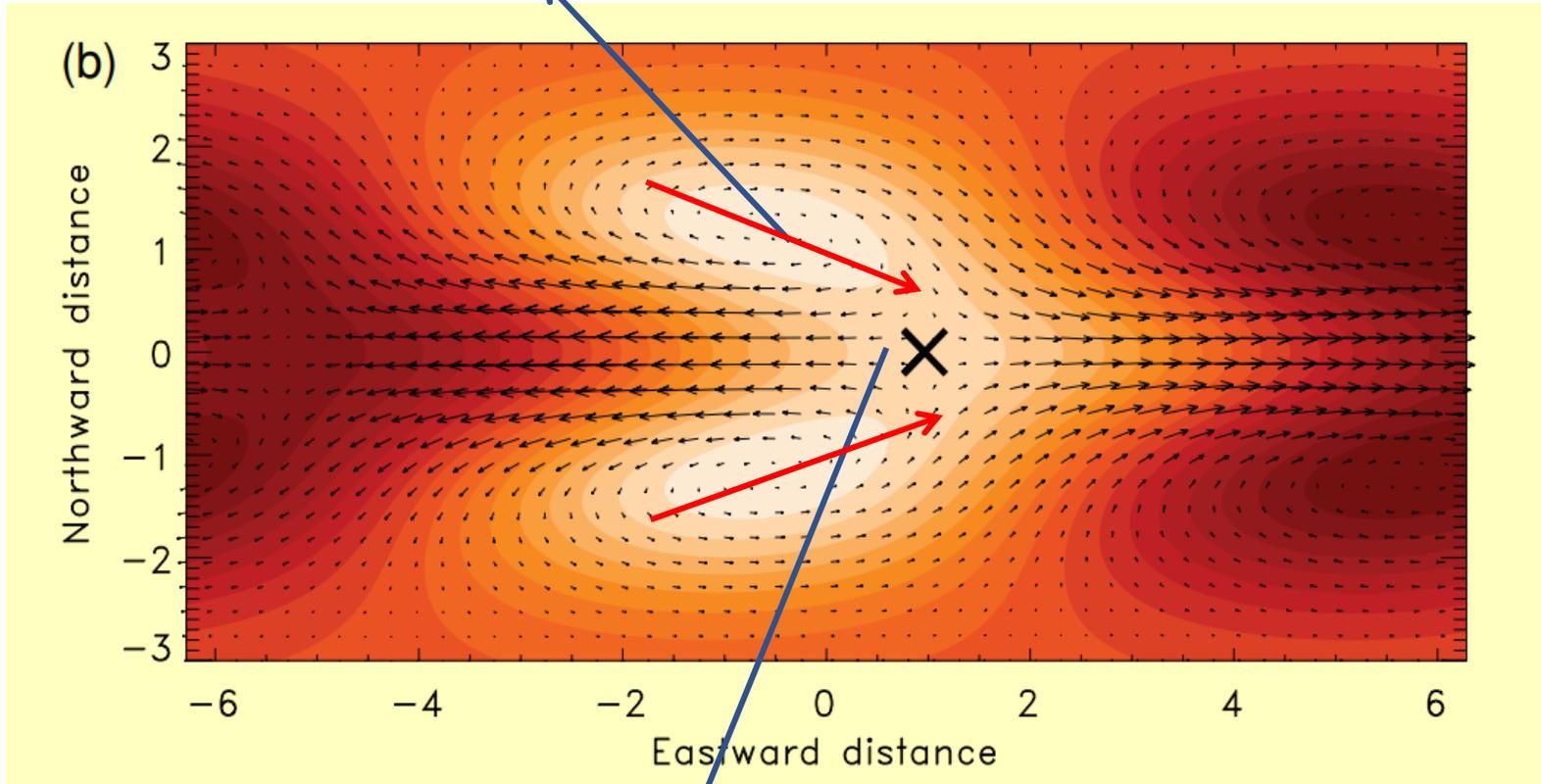
Rossby wave,  $n = 1$  + Kelvin wave,  $n = -1$



Matsuno, 1966, JMSJ

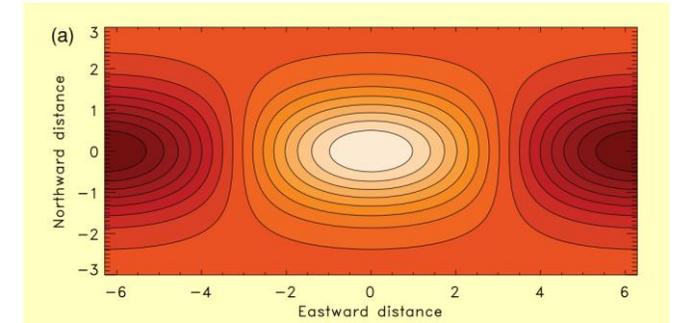
# HD Mechanism: Momentum transport

Westward propagating Rossby wave



Showman & Polvani, 2011, ApJ

Eastward propagating Kelvin wave  eastward hotspot



Gaussian thermal forcing

Velocity Tilting



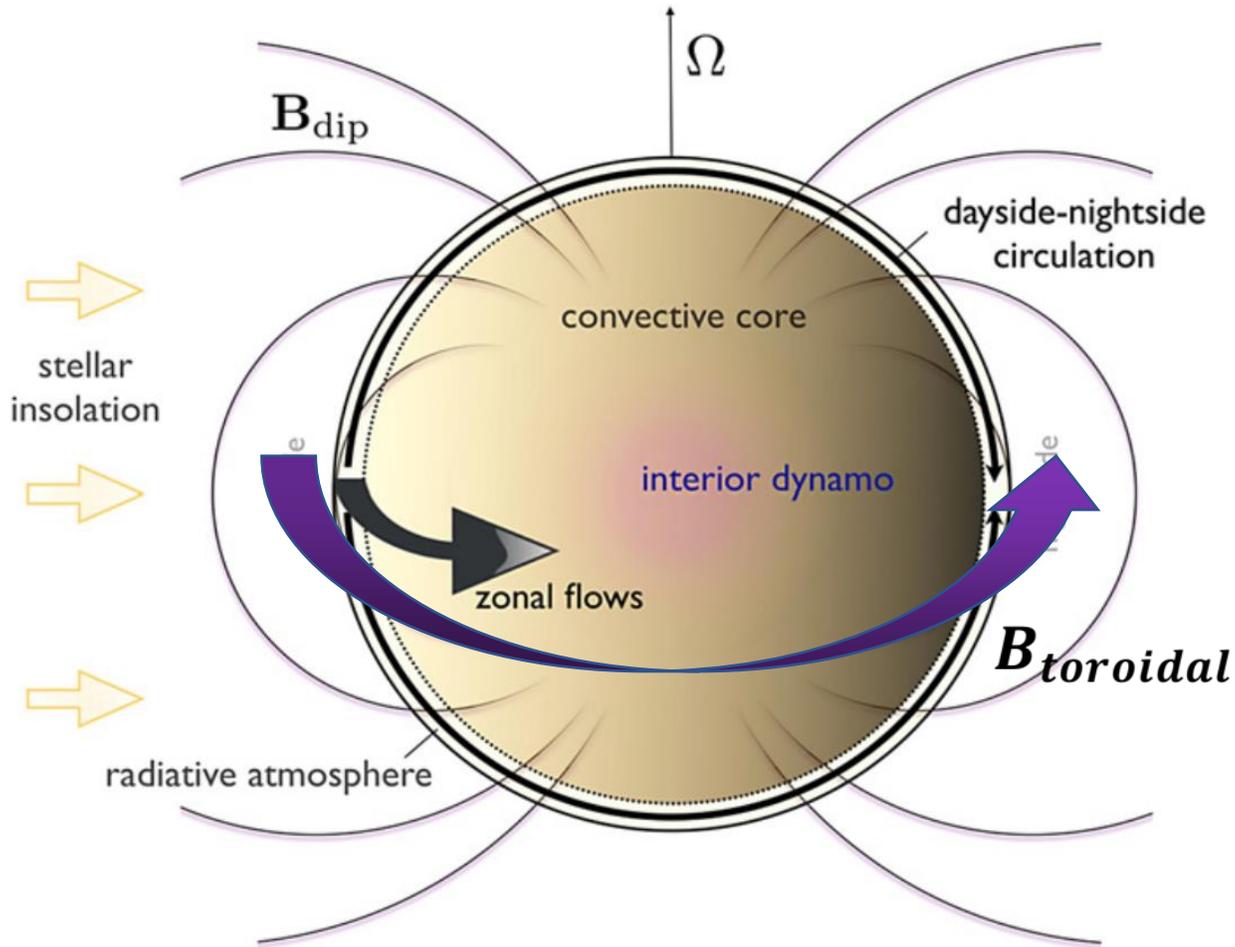
Momentum transport from high latitude to equator



Superrotation

# Magnetohydrodynamic: Magnetic field

An analogy to solar Jupiter.



Batygin, 2013, ApJ

Deep-seated dynamo in Hot Jupiters, which contributes to a dipole magnetic field.



Strong Zonal flow interacts with the dipole magnetic field.



Induce another toroidal magnetic field

$$B_{toroidal} \propto \cos\theta \sin\theta$$

$B_{toroidal} \gg B_{dip}$  when temperature is sufficiently high ( $>1600K$ )

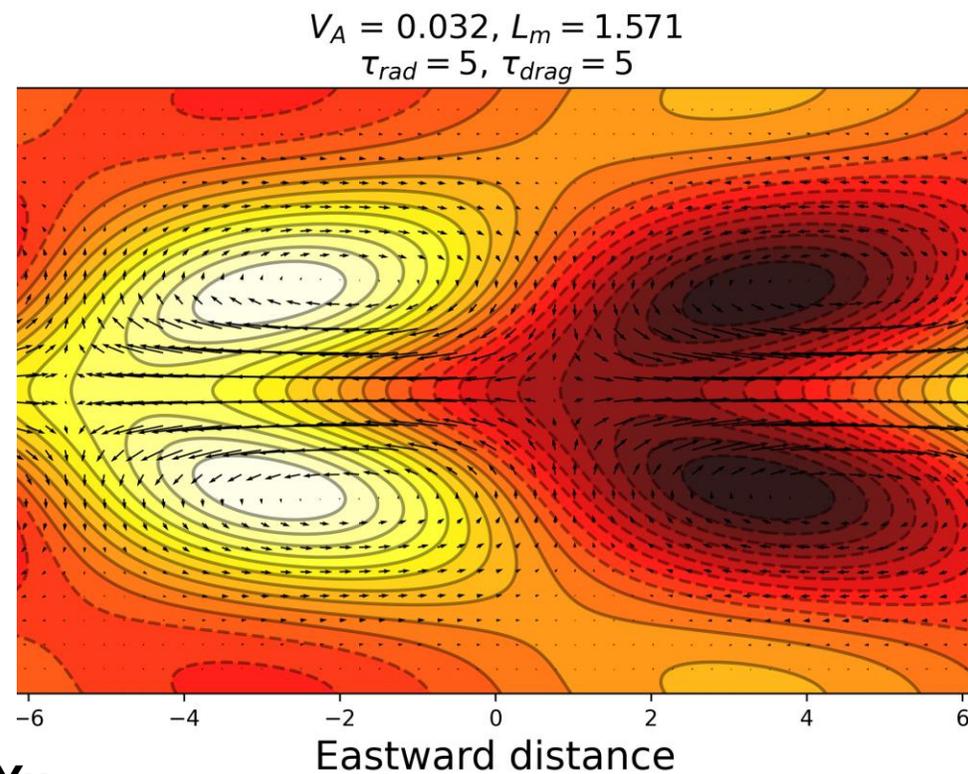
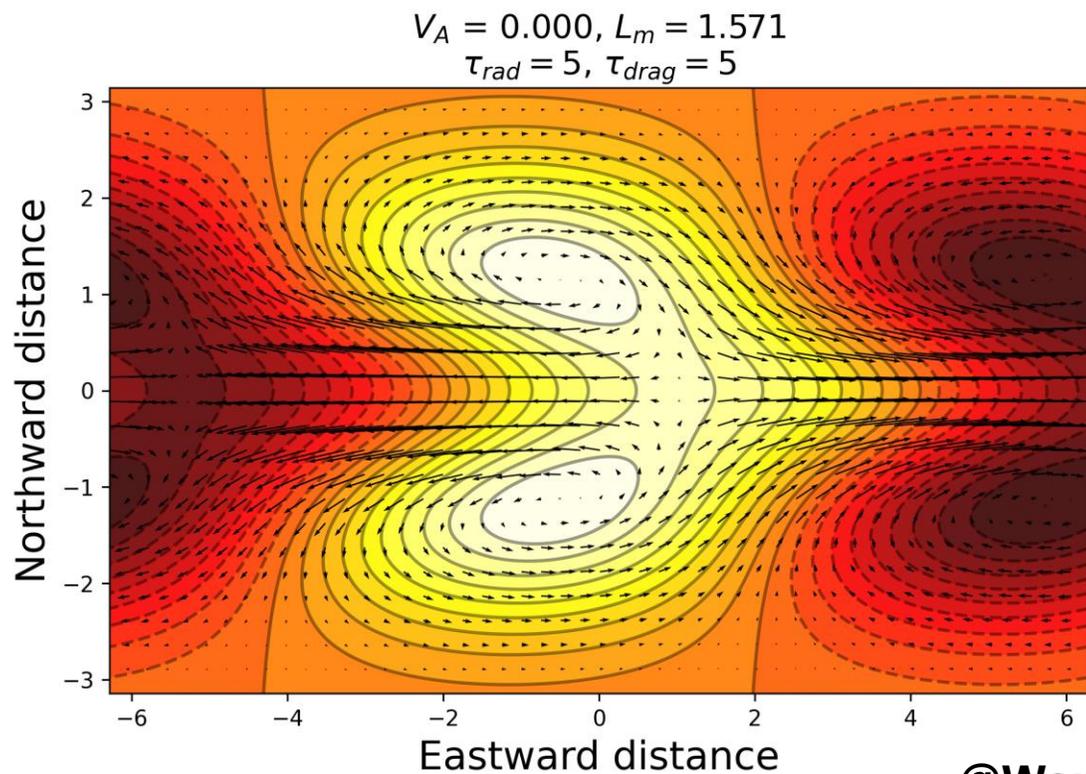


What we use in practice:

$$B_y = 0$$

$$B_{x0} = e^{1/2} V_A \frac{y}{L_m} e^{-y^2/2L_m^2}$$

# MHD: result



@Wang & Yu

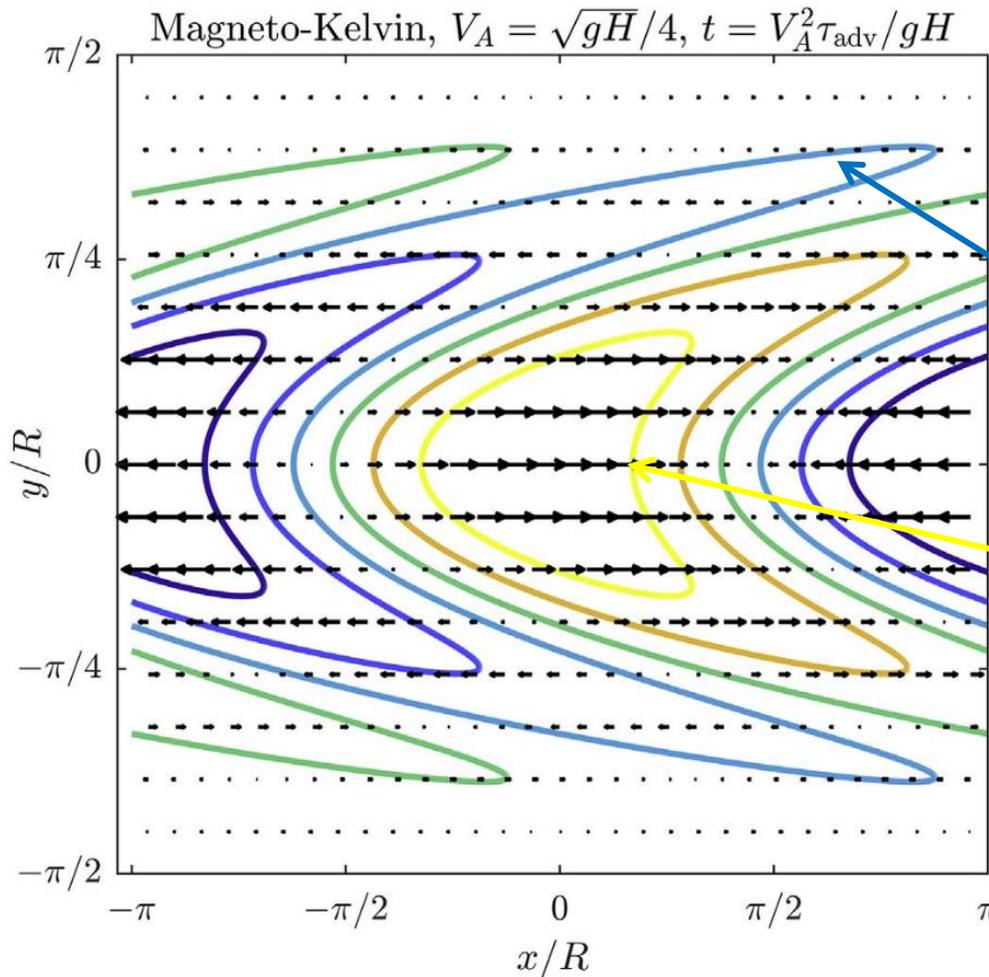
$$B_y = 0$$
$$B_{x0} = e^{1/2} V_A \frac{y}{L_m} e^{-y^2/2L_m^2}$$

Variable:

$V_A$ : Alfvén speed, the strength of magnetic field

$L_m$ : the scale of the magnetic field

# MHD: Deformed Kelvin wave

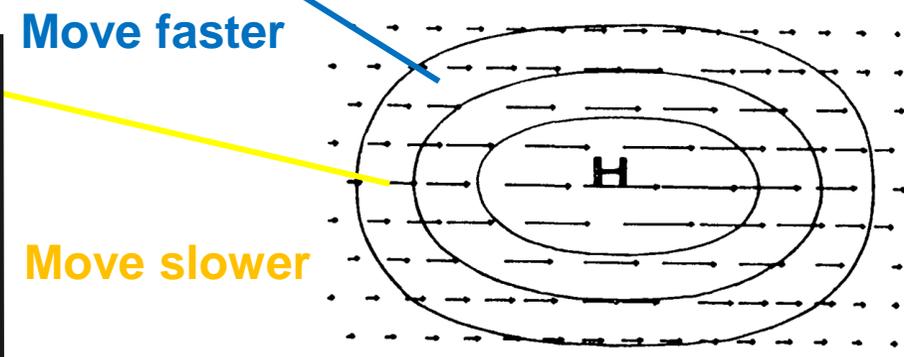


Magnetic field modifies the dispersion relationship

$$\omega = \sqrt{c^2 + v_{A0}^2 \frac{y^2}{R^2}} k_x$$

y dependency

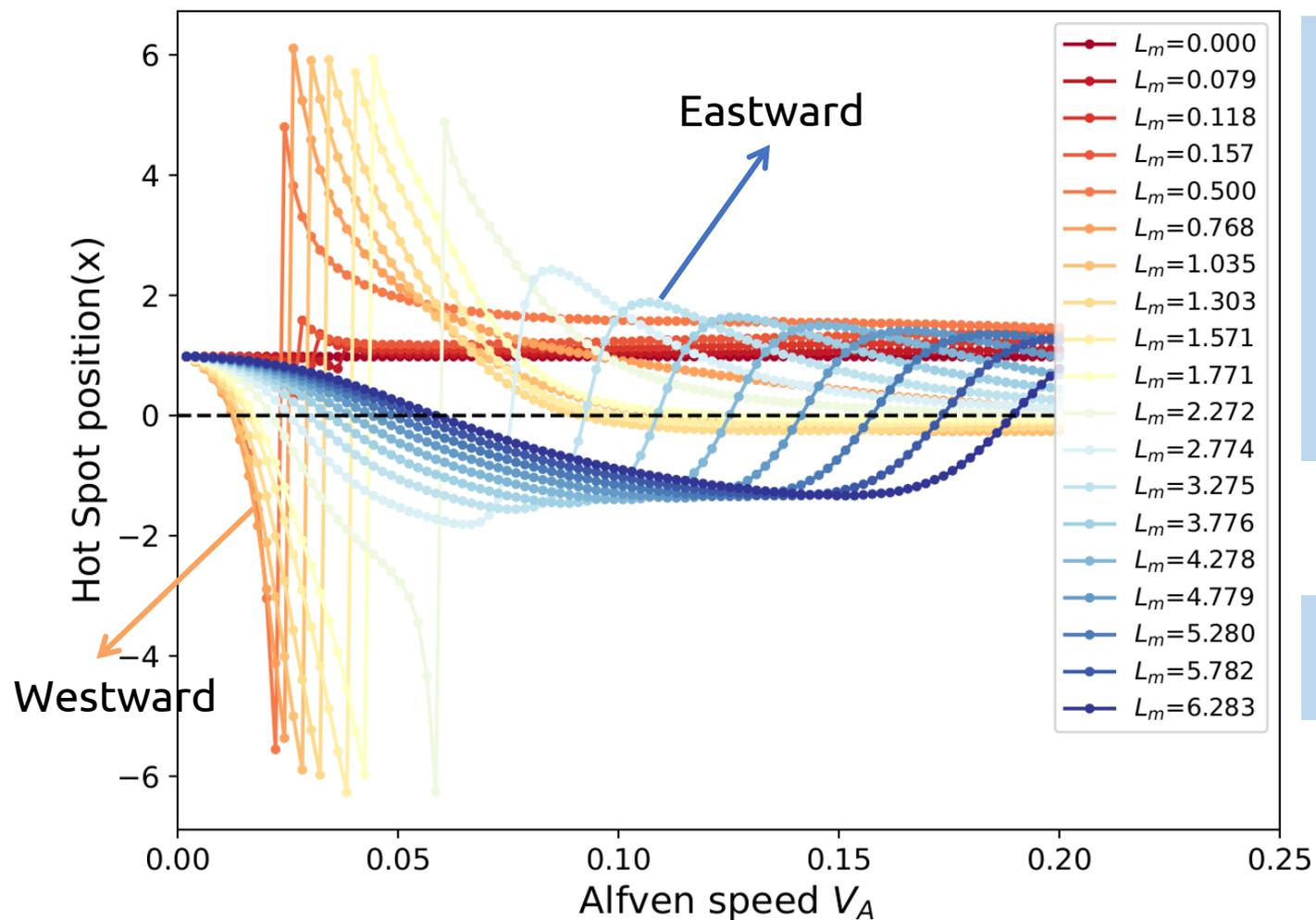
Zaqarashvili, 2018, ApJ



Deformed tilting (Northeast - Southwest)  
 Reversal of wind direction

Hindle et.al, 2019, ApJL

# MHD: Parameter dependency



@Wang & Yu

## Red curve region:

$L_m$  too small, no westward shift ~ Purely HD case

## Yellow and Blue curve region:

$L_m$  moderate, westward shift when  $V_A$  moderate, eastward shift when  $V_A$  very strong

## Weak magnetic field:

Deformed Kelvin wave reverse the wind.

# MHD: Parameter dependency

**Strong magnetic field:**

Magnetic drag dominate, waves can hardly propagate.

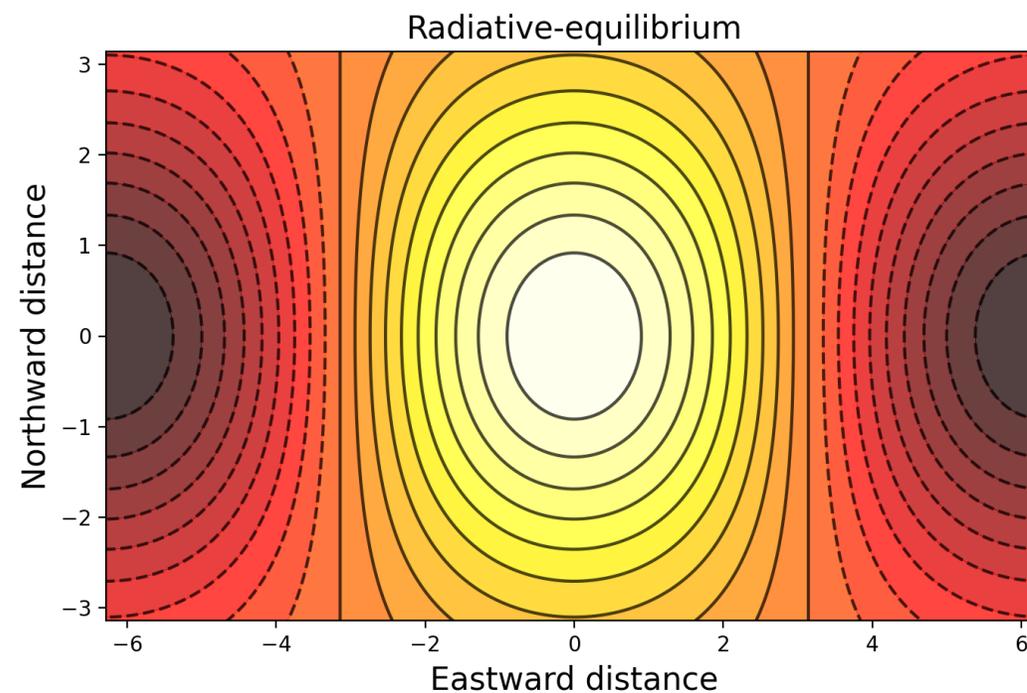
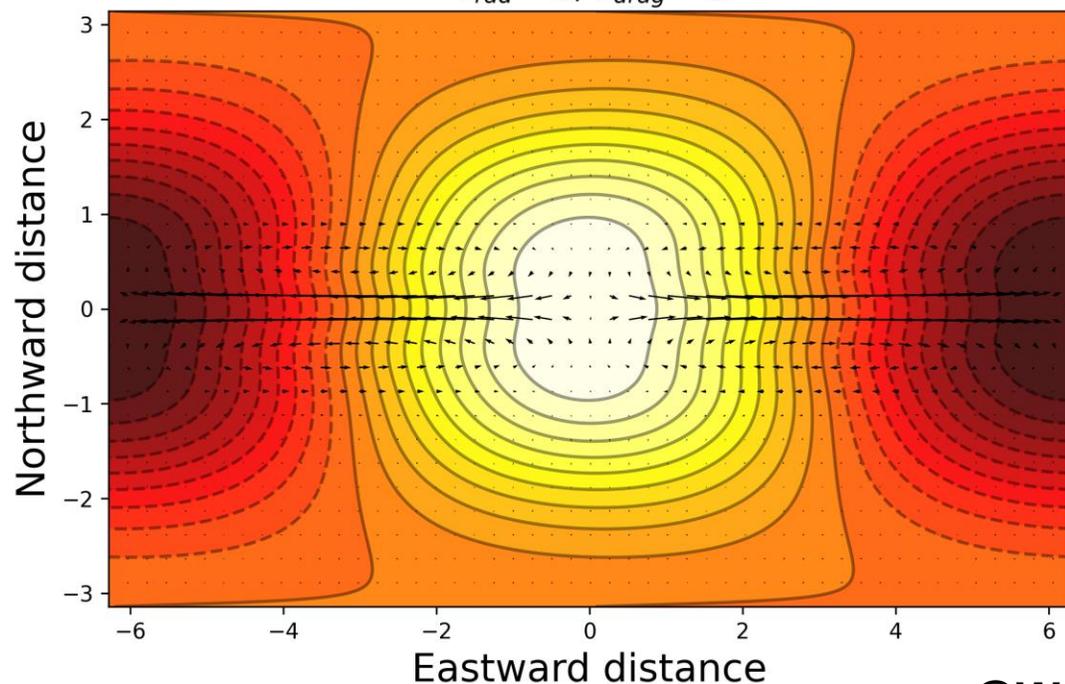
approach



radiative-equilibrium pattern

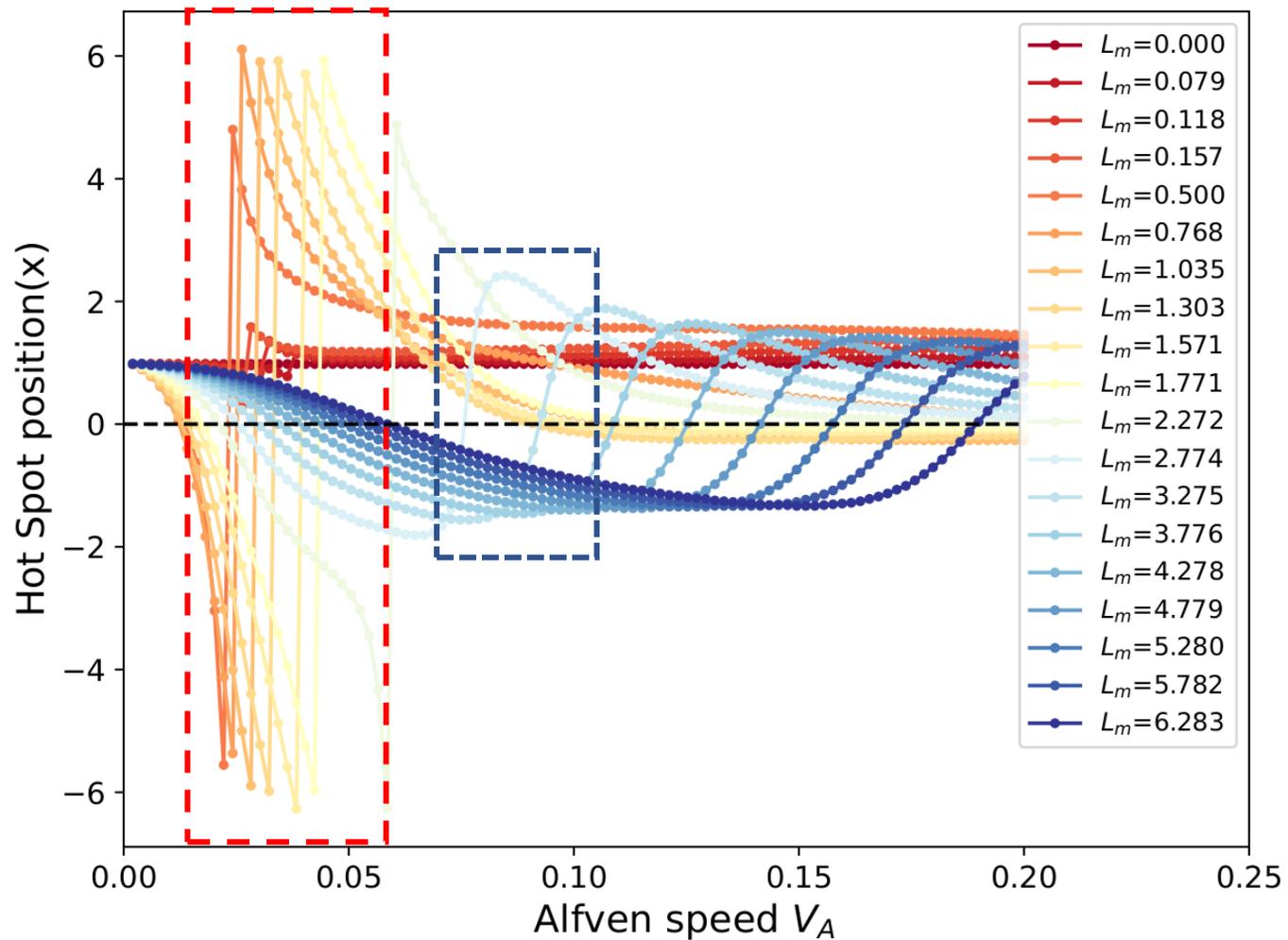
Hotspots don't really shift.

$V_A = 0.200, L_m = 1.571$   
 $\tau_{rad} = 5, \tau_{drag} = 5$



@Wang & Yu

# MHD: Parameter dependency



@Wang & Yu

Rapid transition in hotspot position,  
**Why?**

**Unknown yet...**

Possible idea:  
Dominate wave mode jumps.

Open to any ideas!

# Future work

- Try to explain the mechanism from wave mode splitting.
- We don't consider the impact that equatorial zonal flow may react on waves in turn. (wave-mean flow interaction.) Linking the mean flow to the strength of magnetic field would give a more realistic scenario. (Ref: Hammond 2018, wave-mean; Menou 2012, magnetic scaling law)

# Reference

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- Kevin Heng and Adam P. Showman, “Atmospheric Dynamics of Hot Exoplanets,” *Annual Review of Earth and Planetary Sciences* 43, no. 1 (2015): 509–40.
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Thanks for listening